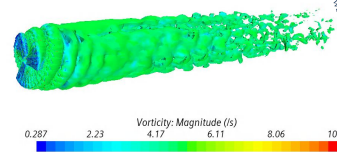


J. Karpinski<sup>1</sup>, P. Ramaprabhu<sup>1</sup>, K. Granlund<sup>2</sup>, M. Bryant<sup>2</sup>, A. Mazzoleni<sup>2</sup>  
<sup>1</sup>University of North Carolina, Charlotte, NC 28223  
<sup>2</sup>North Carolina State University, Raleigh, NC 27695

The vorticity generated in the wake varies with inlet and machine turbulence



**Peak turbulence**  
 $\sqrt{I_0^2 + I_m^2}$

**Background**

Tethered coaxial, counter-rotating turbines offer the advantage of operating in zero-net torque mode to avoid tether twisting and entanglements. The optimization of single- and multiple coaxial devices for power generation requires insights into wake behavior and advances in low-order wake modeling.

**Project Objectives**

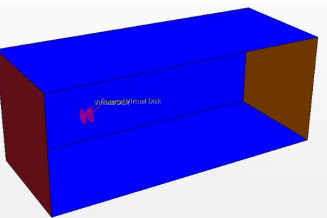
- To use Large Eddy Simulations to develop insights into the evolution of the wake from a tethered turbine across a range of operating conditions and inlet turbulence
- Develop a low-order model for power extraction and wake growth, for the above described conditions.

**Challenges**

- The counter-rotating operation of the rotor tandem in a coaxial turbine creates complex flow conditions in the wake, such as swirl, enhanced levels of turbulence etc.
- Tethered turbines will be deployed in OCT farms, therefore modeling tools must be capable of accurately describing wake interaction between individual units at reasonable computational cost

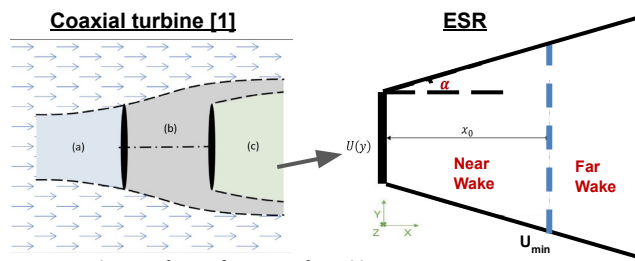
**Our Approach**

- We propose to characterize the wake of a fully-modelled coaxial turbine using a low-order model for an **Equivalent Single Rotor (ESR)**



**LES Parameters**  
 D = 0.2 m  
 Length = 20D  
 Height = 8D  
 Width = 8D  
 $U_{mean} = 1 \text{ m/s}$   
 Distance Between Disks = 0.5D

An ESR is defined as an equivalent single rotor, defined by its induction factor, that extracts the same relative power from the mean flow as a dual-rotor coaxial turbine, while injecting the same amount of turbulence into the wake



Induction factor for ESR is found by requiring:

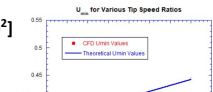
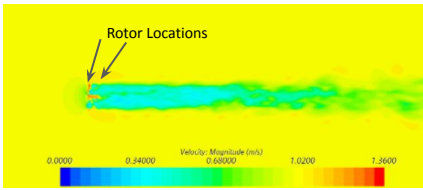
$$C_{P,ESR} = C_{P,W} + C_{P,L}$$

$$4a_{ESR}(1-a_{ESR})^2 = 4[(1-a_w)^2 + (1-a_l)^2(a_l - 2a_w)^2]$$

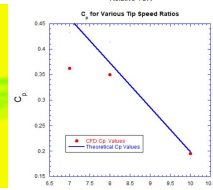
Solve for  $a_{ESR}$

**Validation**

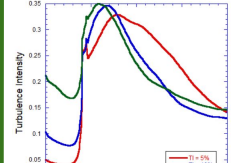
- ESR approach is validated from comparing the wake structure from LES of a coaxial turbine with results from simulation of a single rotor, but operating with an induction factor of the corresponding ESR,  $a_{ESR}$



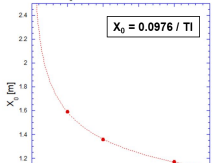
$$U_{min} = U_0(1-2a_{ESR})$$



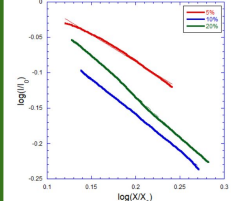
**Turbulence Intensity vs. Distance**



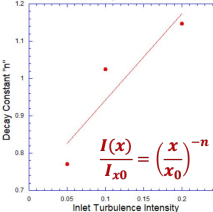
**X<sub>w</sub> vs. Turbulence Intensity**



**Log-Log Turbulence Decay**



**Turbulence Decay vs. Inlet Turbulence**



**Turbulence Effects**

- A coaxial turbine exposed to a higher inlet turbulence produces a higher maximum turbulence intensity (TI), leading to faster wake recovery
- This peak occurs sooner for higher inlet TI
- Our LES show turbulent decay rate also increases linearly with inlet TI
- Breakdown of vortex structures earlier for higher turbulence

Linear fit:  $n = 2.3218 \cdot TI + 0.70966$

**Conclusions**

- The LES results for coaxial turbines at varying inlet turbulence levels provide insight into the wake behavior resulting from the interaction between blades. We have developed a wake model based on an Equivalent Single Rotor, and validated model predictions (power prediction, wake growth rates) with results from Large Eddy Simulations.
- ESR model can be extended to capture wake interactions between multiple turbines in an OCT farm.

**Acknowledgements**

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**References:**

[1] R. Metoyer et al., Ocean Engineering, 215, 107877 (2020).